

## **Computer Vision using Ruby and libJIT**

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### **Published version**

WEDEKIND, Jan (2009). Computer Vision using Ruby and libJIT. In: RubyConf 2009, San Francisco, California.

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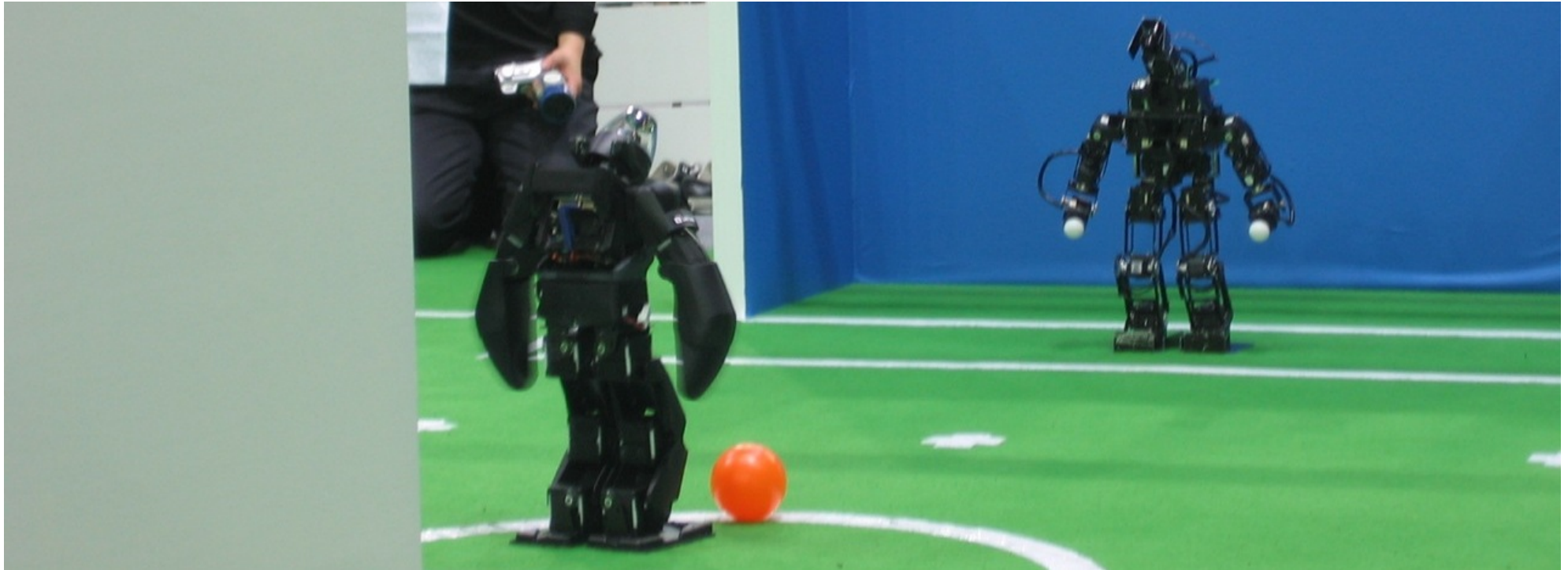
## RubyConf 2009

# Computer Vision using Ruby and libJIT

Jan Wedekind

Thu Nov 19 13:15:00 PST 2009

Embassy Suites San Francisco Airport, Room 1



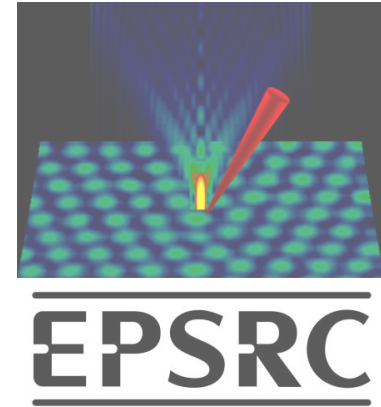
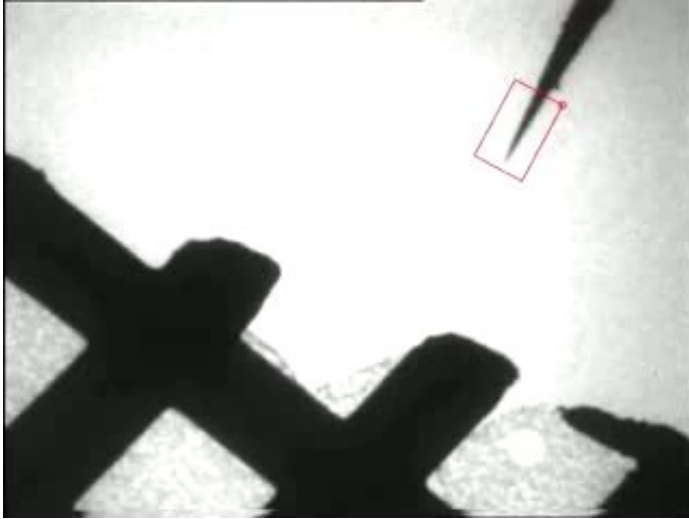
<http://www.flickr.com/photos/schoschie/171544759/>





# Background


## EPSRC Nanorobotics Project



<http://vision.eng.shu.ac.uk/mmvwiki/index.php/Nanorobotics>

<http://nano.group.shef.ac.uk/>



[illegible]


http://shuttle52.zm1-home-back-zones-MozillaFirefox... Close

### Back Zones

Id	Name	Type	Area (sq./m)	Mark
4.	Surface	Active	64041 / 69.17	<input type="checkbox"/>
6.	Zone	Inactive	24429 / 26.17	<input type="checkbox"/>
67.	Boule	Active	2249 / 2.22	<input type="checkbox"/>
26.	Prachu	Preliminary	2091 / 2.06	<input type="checkbox"/>

Add New Zone Close

Done Addback



3/47



# The Array Challenge

## Computer Vision means Array Operations

### C/C++

```
#include <stdlib.h>
#define SIZE 100000000
int main(void)
{
    int i, *arr = (int *)
        malloc( SIZE *
                sizeof(int) );
    for ( i = 0; i < SIZE; i++ )
        arr[ i ] = i;
    free( arr );
    return 0;
}
```

**gcc 4.2.4 0.06s**

### Ruby

```
SIZE = 100000000
arr = ( 0 ... SIZE ).
    collect { |i| i }
```

**ruby 1.8.6 76.3s**

**ruby 1.9.1 1.8s**

Intel® Core™2 CPU T5600 @ 1.83GHz

Linux 2.6.24-24-generic SMP i686 GNU/Linux



## Maybe we shouldn't use Ruby here?



<http://www.imdb.com/title/tt0343818/>

# Expressiveness (multi-dimensional '+')

## C++ and Boost::MultiArray



```
#include <boost/multi_array.hpp> // 3726 lines of code
#include <iostream>
using namespace boost;
template< typename T >
T &multi_plus( T &a, const T &b, const T &c )
{
    a = b + c;
    return a;
}

template< template< typename, size_t, typename > class Arr,
           typename Alloc, typename T, size_t N >
detail::multi_array::sub_array< T, N > multi_plus
( detail::multi_array::sub_array< T, N > a,
  const Arr< T, N, Alloc > &b, const Arr< T, N, Alloc > &c )
{
    typename Arr< T, N, Alloc >::const_iterator j = b.begin();
    typename Arr< T, N, Alloc >::const_iterator k = c.begin();
    for ( typename detail::multi_array::sub_array< T, N >::
          iterator i = a.begin(); i != a.end(); i++, j++, k++ )
        multi_plus( *i, *j, *k );
    return a;
}

template< template< typename, size_t, typename > class Arr,
           typename Alloc, typename T, size_t N >
Arr< T, N, Alloc > &multi_plus
( Arr< T, N, Alloc > &a,
  const Arr< T, N, Alloc > &b, const Arr< T, N, Alloc > &c )
{
    typename Arr< T, N, Alloc >::const_iterator j = b.begin();
    typename Arr< T, N, Alloc >::const_iterator k = c.begin();
    for ( typename Arr< T, N, Alloc >::
          iterator i = a.begin(); i != a.end(); i++, j++, k++ )
        multi_plus( *i, *j, *k );
    return a;
}
```

```
template < template< typename, size_t, typename > class Arr,
           typename Alloc, typename T, size_t N >
multi_array< T, N > operator+
( const Arr< T, N, Alloc > &a,
  const Arr< T, N, Alloc > &b )
{
    array< size_t, N > shape;
    std::copy( a.shape(), a.shape() + N, shape.begin() );
    multi_array< T, N > retVal( shape );
    multi_plus( retVal, a, b );
    return retVal;
};

int main(void)
{
    multi_array< int, 2 > a( extents[ 2 ][ 2 ] );
    a[0][0] = 1; a[0][1] = 2; a[1][0] = 3; a[1][1] = 4;
    multi_array< int, 2 > b( extents[ 2 ][ 2 ] );
    b[0][0] = 5; b[0][1] = 4; b[1][0] = 3; b[1][1] = 2;
    multi_array< int, 2 > r( a + b );
    std::cout << "[ [ " << r[0][0] << ", " << r[0][1]
               << " ], [ " << r[1][0] << ", " << r[1][1]
               << " ] ]" << std::endl;
    // [ [ 6, 6 ], [ 6, 6 ] ]
    return 0;
}
```

# Expressiveness (multi-dimensional '+')

## Ruby and Standard Library

```
class Array
  def +( other )
    zip( other ).collect { |x,y| x + y }
  end
end

a = [ [ 1, 2 ], [ 3, 4 ] ]
b = [ [ 5, 4 ], [ 3, 2 ] ]
puts ( a + b ).inspect
# [ [ 6, 6 ], [ 6, 6 ] ]
```

straightforward!





# Implementation

## Uniform Arrays



[  ,  ,  ,  ,  ,  ,  , ... ]

Also see: [NArray](#)



# Implementation

## Malloc Objects

```
m = Malloc.new 10
m.write '0123456789'
# "0123456789"
m.read 5
# "01234"
( m + 2 ).read 5
# "23456"
```



# Implementation

## Using 'Array#pack' and 'String#unpack'

```
class INT
  def initialize( v = 0 )
    @malloc = Malloc.new 4
    set v
  end
  def inspect
    "#{ self.class.inspect }(#{ get })"
  end
  def set( v = 0 )
    @malloc.write [ v ].pack( 'i' )
    v
  end
  def get
    @malloc.read( 4 ).unpack( 'i' )[ 0 ]
  end
end
```

```
i = INT.new 3
# INT(3)
i.set 5
# 5
i
# INT(5)
i.get
# 5
```



# Implementation

## Type System: Generic Native Scalar

```
class INT_  
  class << self  
    attr_accessor :bits  
    attr_accessor :signed  
  end  
  # ...  
end  
SIGNED = true  
UNSIGNED = false  
def INT( bits, signed )  
  retval = Class.new INT_  
  retval.bits = bits  
  retval.signed = signed  
  retval  
end
```

```
USINT = INT 16, UNSIGNED  
# USINT  
u = USINT.new 3  
# USINT(3)  
v = USINT.new u.malloc  
# USINT(3)
```





# Implementation

## Type System: Native Arrays

```
class Sequence_
  class << self
    attr_accessor :elem, :num,
                  :stride

  end
  # ...
  def sel( i )
    elem.new @malloc + i *
              elem.bytes * stride
  end
  def []( i )
    sel( i ).get
  end
  def []=( i, v )
    sel( i ).set v
  end
end
```

```
SINT = INT 16, SIGNED
# SINT
s = Sequence( SINT, 8 ).new.fill!
# Sequence(SINT,8):
# [ 0, 0, 0, 0, 0, 0, 0, 0 ]
s[ 3 ] = 5
# 5
s
# Sequence(SINT,8):
# [ 0, 0, 0, 5, 0, 0, 0, 0 ]
s[ 3 ]
# 5
s.sel 3
# SINT(5)
```



# Implementation

## Type System: Recursive Arrays

```
M = Sequence( Sequence( INT( 32, SIGNED ), 3 ), 2 )
# MultiArray.int(3,2)
m = M.new.fill! 1
# MultiArray.int(3,2):
# [ [ 1, 1, 1 ],
#   [ 1, 1, 1 ] ]
m[ 1 ]
# Sequence.int(3):
# [ 1, 1, 1 ]
m[ 2, 1 ]
# 1
m[ 1 ][ 2 ] = 0
# 0
m[ 1 .. 2, 0 .. 1 ]
# MultiArray.int(2,2):
# [ [ 1, 1 ],
#   [ 1, 0 ] ]
```





# Array Operations





# Implementation

## Array Operations: Scalar Operations

```
module RubyScalar
  def op( *args, &action )
    instance_exec *args, &action
    self
  end
  def -@
    self.class.new.op( get ) { |x| set -x }
  end
  # ...
end

class INT_
  include RubyScalar
end
```

```
i = SINT.new 3
# SINT(3)
-i
# SINT(-3)
```





# Implementation

## Array Operations: Element-Wise Array Operations

```
module RubySequence
  def op( *args, &action )
    for i in 0 ... num
      subargs = args.collect do |v|
        v.is_a?( Sequence_ ) ? v[ i ] : v
      end
      sel( i ).op *subargs, &action
    end
    self
  end
  def -@
    self.class.new.op( get ) { |x| set -x }
  end
end

class Sequence_
  include RubySequence
end
```

```
S = Sequence( INT, 3 )
# Sequence.int(3)
s = S.new.indgen!
# Sequence.int(3):
# [ 0, 1, 2 ]
-s
# Sequence.int(3):
# [ 0, -1, -2 ]
```



# How to speed-up things?





# Implementation

## Reflection in Ruby: Example

```
class Const
  attr_accessor :inspect
  alias_method :to_s, :inspect
  def initialize( s )
    @inspect = s.to_s
  end
  def method_missing( name, *args )
    str = "#{ self }.#{ name }"
    unless args.empty?
      str += "( #{args.join ', ' } )"
    end
    Const.new str
  end
  def coerce( y )
    return Const.new( y ), self
  end
end
```

```
a = Const.new 'a'
# a
b = Const.new 'b'
# b
-a
# a.-@
a + b
# a.+( b )
a[ 2 ]
# a[]( 2 )
2 * a
# 2.*( a )
2 * a + b
# 2.*( a ).+( b )
2 * ( a + b )
# 2.*( a.+( b ) )
```



# Implementation

## Reflection in Ruby: Limitations

```
a or b
# a

a < b ? a : b
# a

b = a
# a

if a > b
  a -= b
end
# a.-( b )

begin
  a += 1
end until a > b
a
# a.+( 1 )
```

```
b and a
# a

a > b ? a : b
# a

x = a
# a

a - b
#
#
# a.-( b )

b = a + 1
#
#
#
# a.+( 1 )
```





# Implementation

## JIT-Compilation: Scalar Operation I/II

```
module JITScalar
  def op( *args, &action )
    if ( [ self ] + args ).all? { |arg| arg.jit_support? }
      JITFunction.jit( self, *args ) do |f, _self, *_args|
        _self.op *_args, &action
      end
    else
      super *args, &action
    end
  end
end

class INT_
  include JITScalar
end
```

'JITFunction.jit': cache, compile, and execute



# Implementation

## JIT-Compilation: Scalar Operation II/II

```
i = INT.new 3
# INT(3)
i.class.new.op( i.get ) do |x|
  puts "self = #{self}"
  puts "x      = #{x}"
  puts
  set -x
end
# self = INT(*i1)
# x      = i2
# INT(-3)
```



```
function -@( i1: ptr,
              i2: int ): void
    i3 = -i2
    *i1 = i3
```

machine code generated by libJIT/ DotGNU

<http://freshmeat.net/projects/libjit/>

Also see: [ruby-libjit](#)



# Implementation

## JIT-Compilation: Array Operation I/V

```
module JITSequence
  def op( *args, &action )
    if ( [ self ] + args ).all? { |arg| arg.jit_support? }
      JITFunction.jit( self, *args ) do |f, _self, *_args|
        _self.op *_args, &action
      end
    self
  elsif is_jit?
    f = malloc.f
    r = JITTerm.value f, JITType::PTR, malloc
    s = stride * elem.bytes
    rend = r + s * num
  end
end
```



# Implementation

## JIT-Compilation: Array Operation II/V

```
extract, increment = [], []
args.each do |arg|
  if arg.is_a? Sequence_
    ptr = JITTerm.value f, JITType::PTR, arg.malloc
    astride = arg.stride * arg.elem.bytes
    extract.push proc { arg.elem.new( ptr ).get }
    increment.push proc { ptr.set ptr + astride }
  else
    extract.push proc { arg }
  end
end
```





# Implementation

## JIT-Compilation: Array Operation III/V

```
f.until( proc { r == rend } ) do
  _subargs = extract.collect { |i| i.call }
  elem.new( r ).op *_subargs, &action
  increment.each { |i| i.call }
  r.set r + s
end
else
  super *args, &action
end
end
end
class Sequence_
  include JITSequence
end
```

Also cumbersome but much more generic!



# Implementation

## JIT-Compilation: Array Operation IV/V

```
s = Sequence( INT, 3 ).new.indgen!  
# Sequence(INT,3):  
# [ 0, 1, 2 ]  
s.class.new.op( s.get ) do |x|  
  puts "self = #{self}"  
  puts "x      = #{x}"  
  puts  
  set -x  
end  
# self = INT(*i7)  
# x      = i13  
# Sequence(INT,3):  
# [ 0, -1, -2 ]
```





# Implementation

## JIT-Compilation: Array Operation V/V

```
function -@( i1:  int, i2:  int, i3:  ptr,  
             i4:  int, i5:  int, i6:  ptr ):  void
```

```
    i7 = i3
```

```
    i8 = i2 * 4
```

```
    i9 = i8 * i1
```

```
    i10 = i7 + i9
```

```
    i11 = i6
```

```
    i12 = i5 * 4
```



```
L0:
```

```
    if i7 == i10 then goto L1
```

```
    i13 = *i11
```

```
        i14 = -i13
```

```
        *i7 = i14
```

```
    i11 = i11 + i12
```

```
    i7 = i7 + i8
```

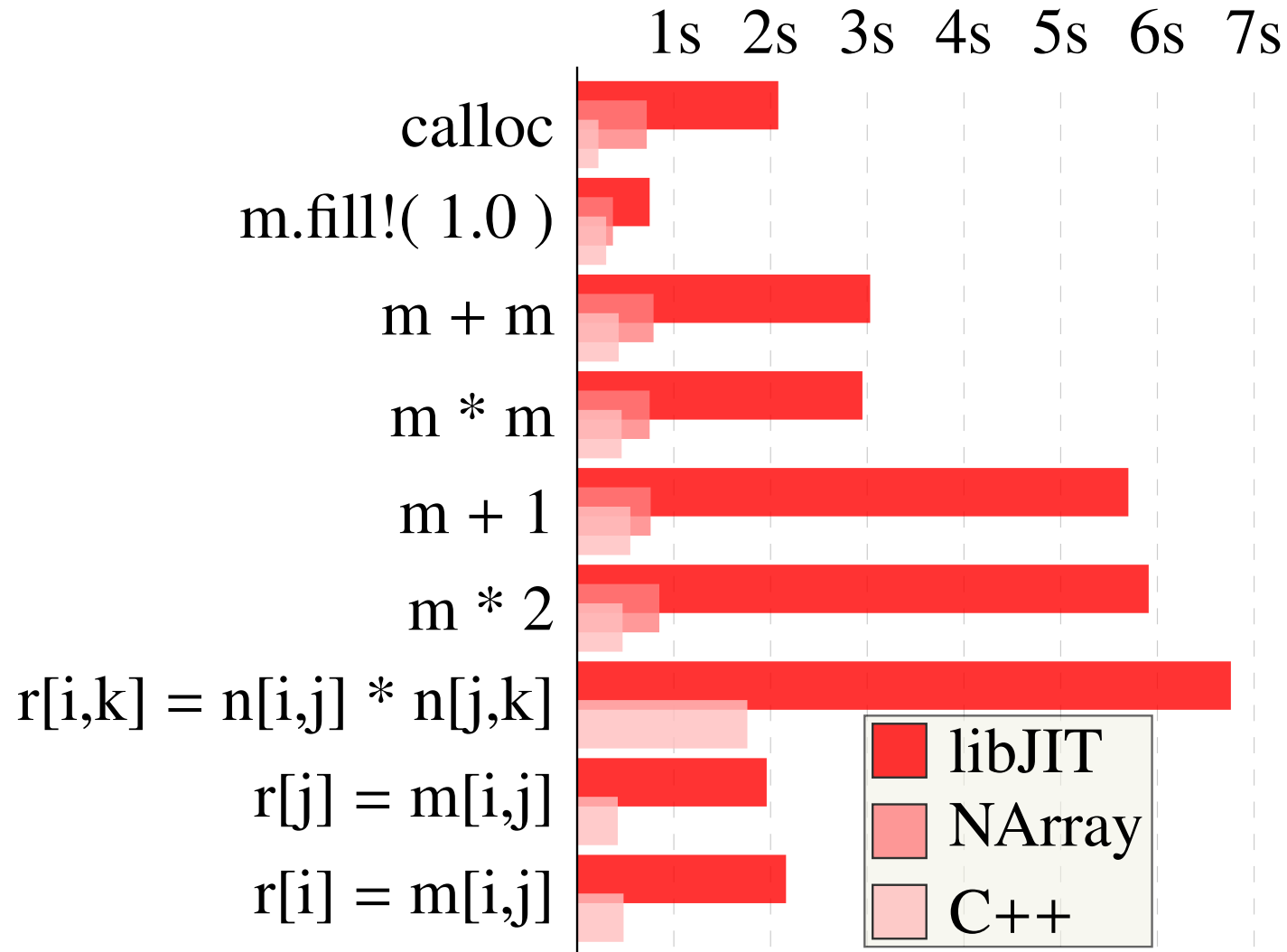
```
    goto L0
```

```
L1:
```



# Implementation

## JIT Results



Intel® Core™2 CPU T5600 @ 1.83GHz

Linux 2.6.24-24-generic SMP i686 GNU/Linux

⇒ future work: prefill cache with GCC code (use [RubyInline](#)?)

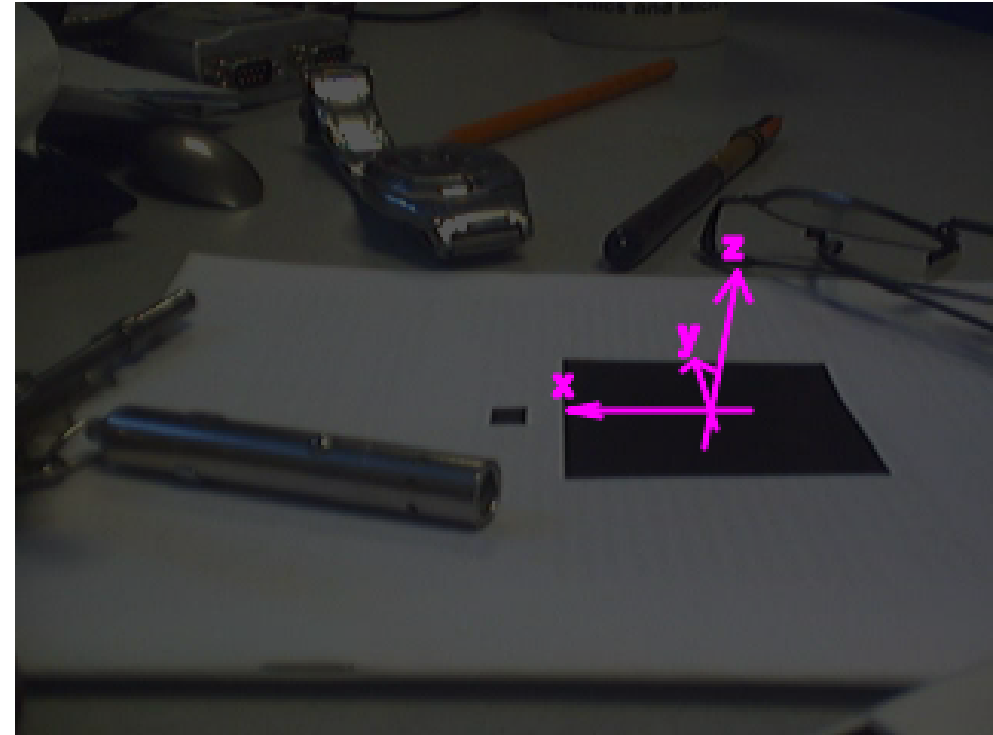


# Augmented Reality Example

**Problem: 3D recognition of planar object**

How to get from here ...

... to here?



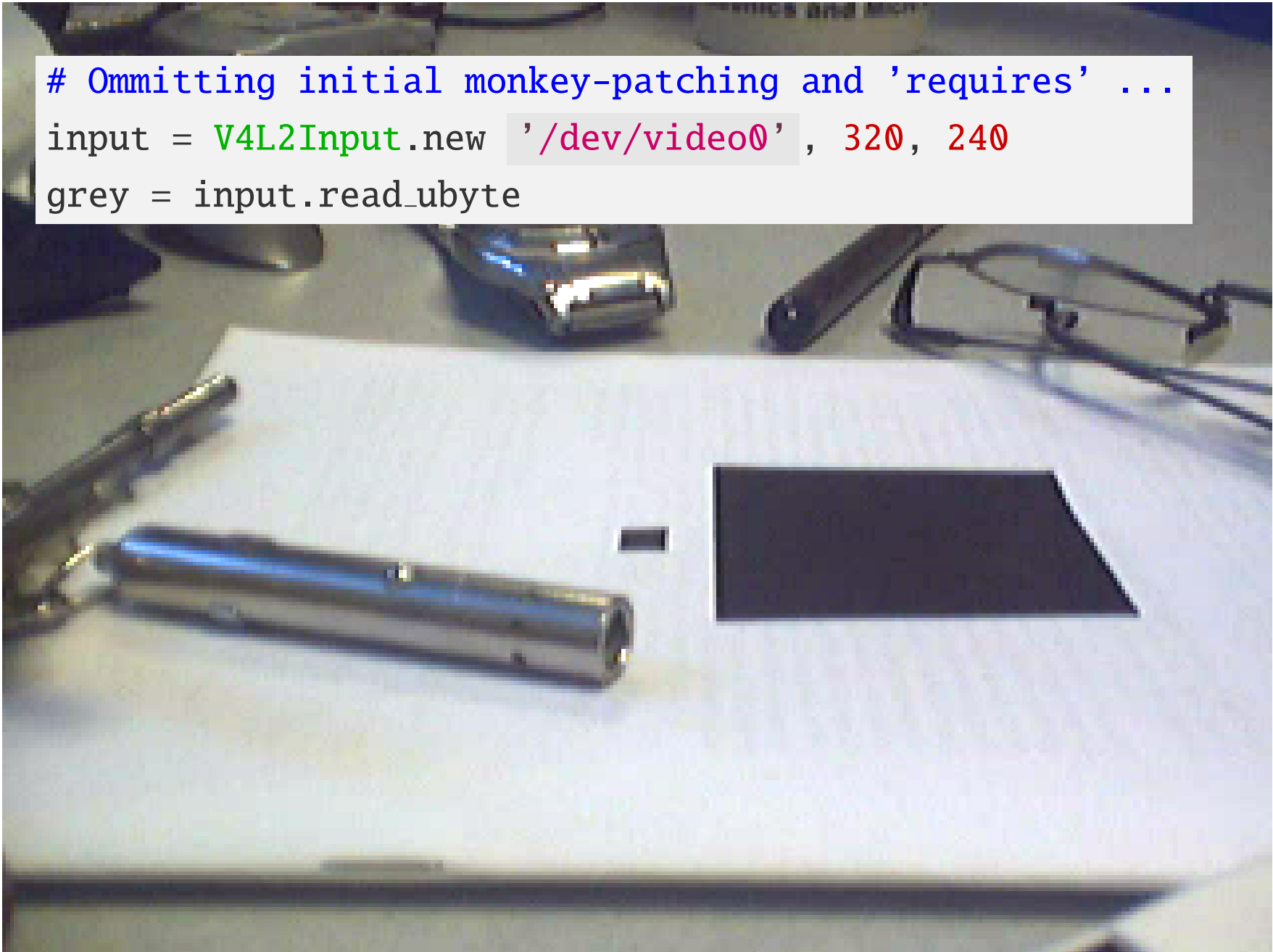




# Augmented Reality Example

## Capture Image

```
# Ommitting initial monkey-patching and 'requires' ...  
input = V4L2Input.new '/dev/video0', 320, 240  
grey = input.read_ubyte
```





# Augmented Reality Example

## Threshold Image

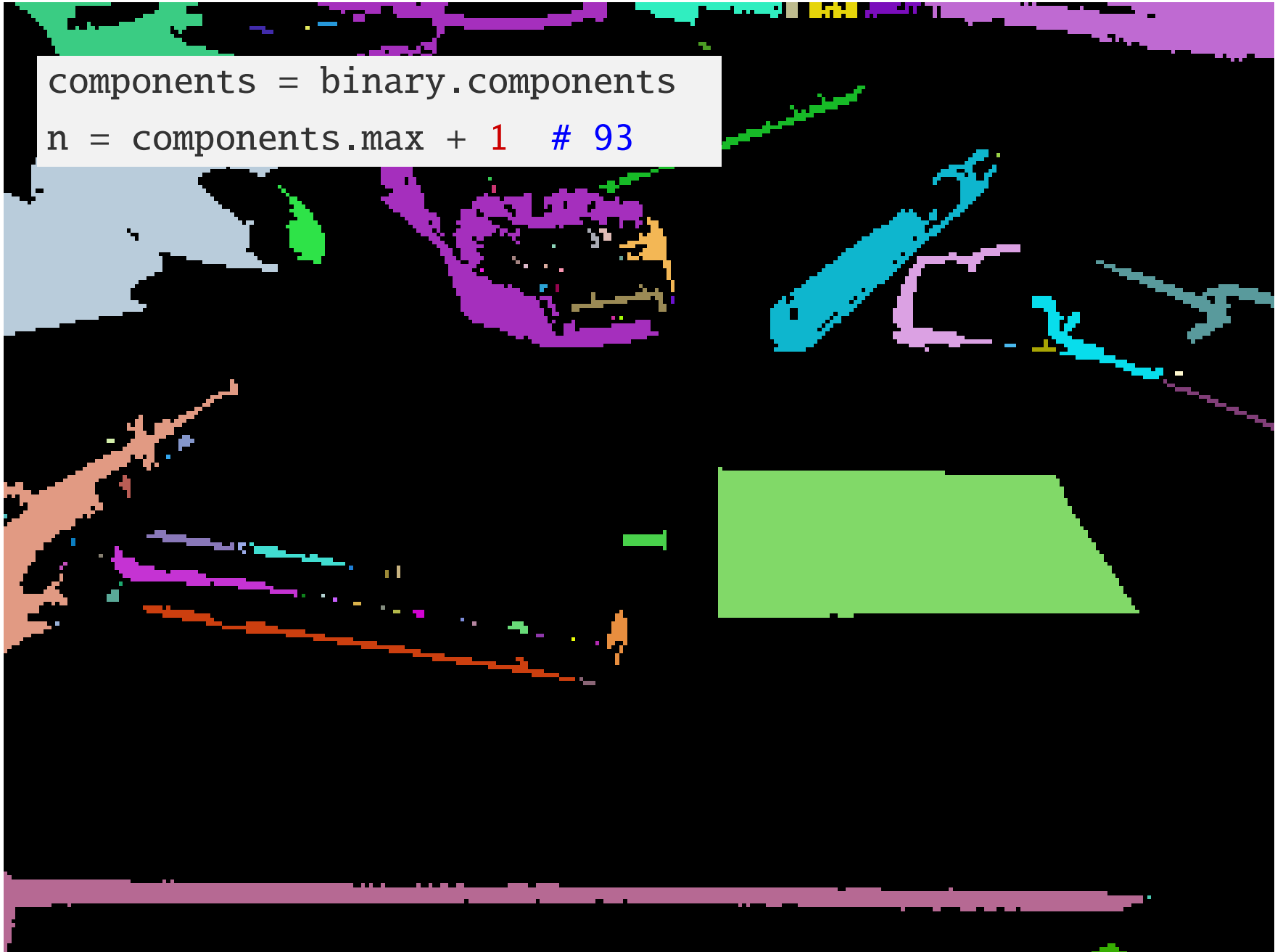




# Augmented Reality Example

## Connected Component Analysis

```
components = binary.components  
n = components.max + 1 # 93
```





# Augmented Reality Example

## Impose Size Constraints

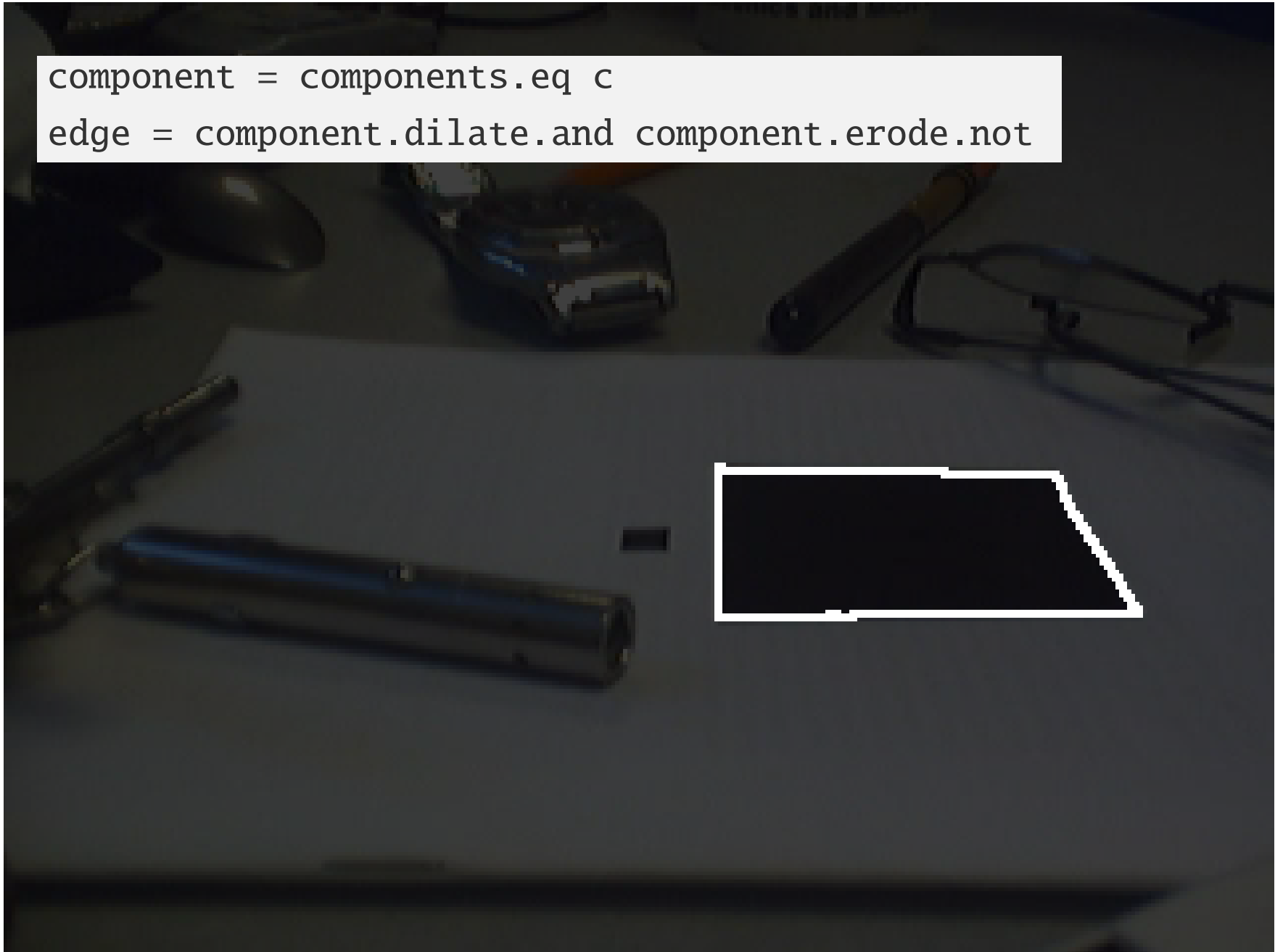
```
range = 30 ** 2 .. 100 ** 2
hist = components.hist n
mask = hist.between? range.min, range.max
Sequence.int( n ).indgen!.mask( mask ).
  to_a.each do |c|
    # c is 27, 47, 56, or 90
    # ...
  end
```



# Augmented Reality Example

## Extract Edge of Component

```
component = components.eq c  
edge = component.dilate.and component.erode.not
```





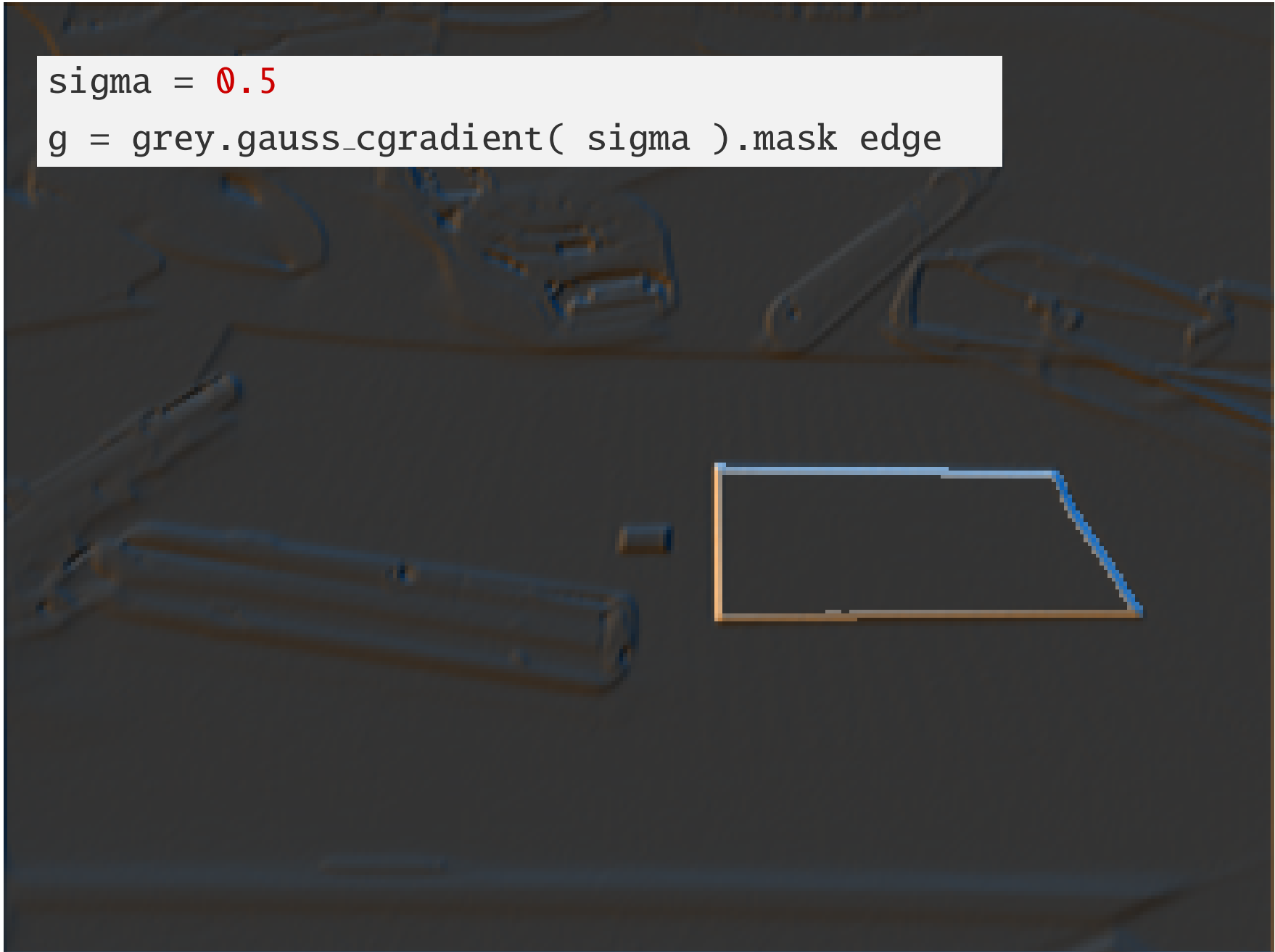


# Augmented Reality Example

## Compute Gradients

```
sigma = 0.5
```

```
g = grey.gauss_cgradient( sigma ).mask edge
```





# Augmented Reality Example

## Group Dominant Orientations

```
q = 36
d_q = ( ( g.arg / Math::PI + 1 ) *
        q / 2 ).to_int % q
d_hist = d_q.hist_weighted q, g.abs
msk = d_hist >= d_hist.max / 4
segments = msk.components
partitions = d_q.map segments
```

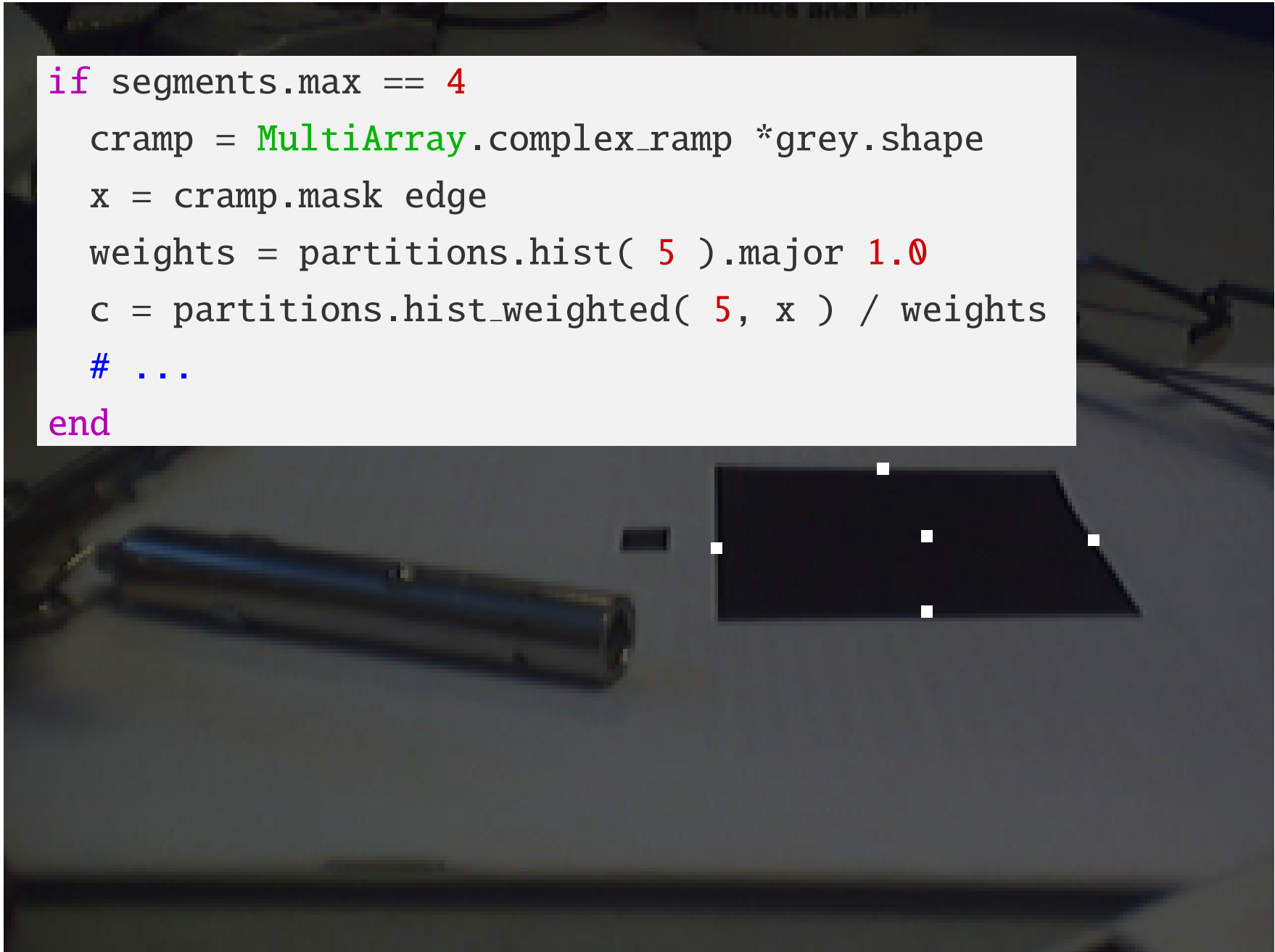




# Augmented Reality Example

## Centre of each Line

```
if segments.max == 4
  cramp = MultiArray.complex_ramp *grey.shape
  x = cramp.mask edge
  weights = partitions.hist( 5 ).major 1.0
  c = partitions.hist_weighted( 5, x ) / weights
  # ...
end
```

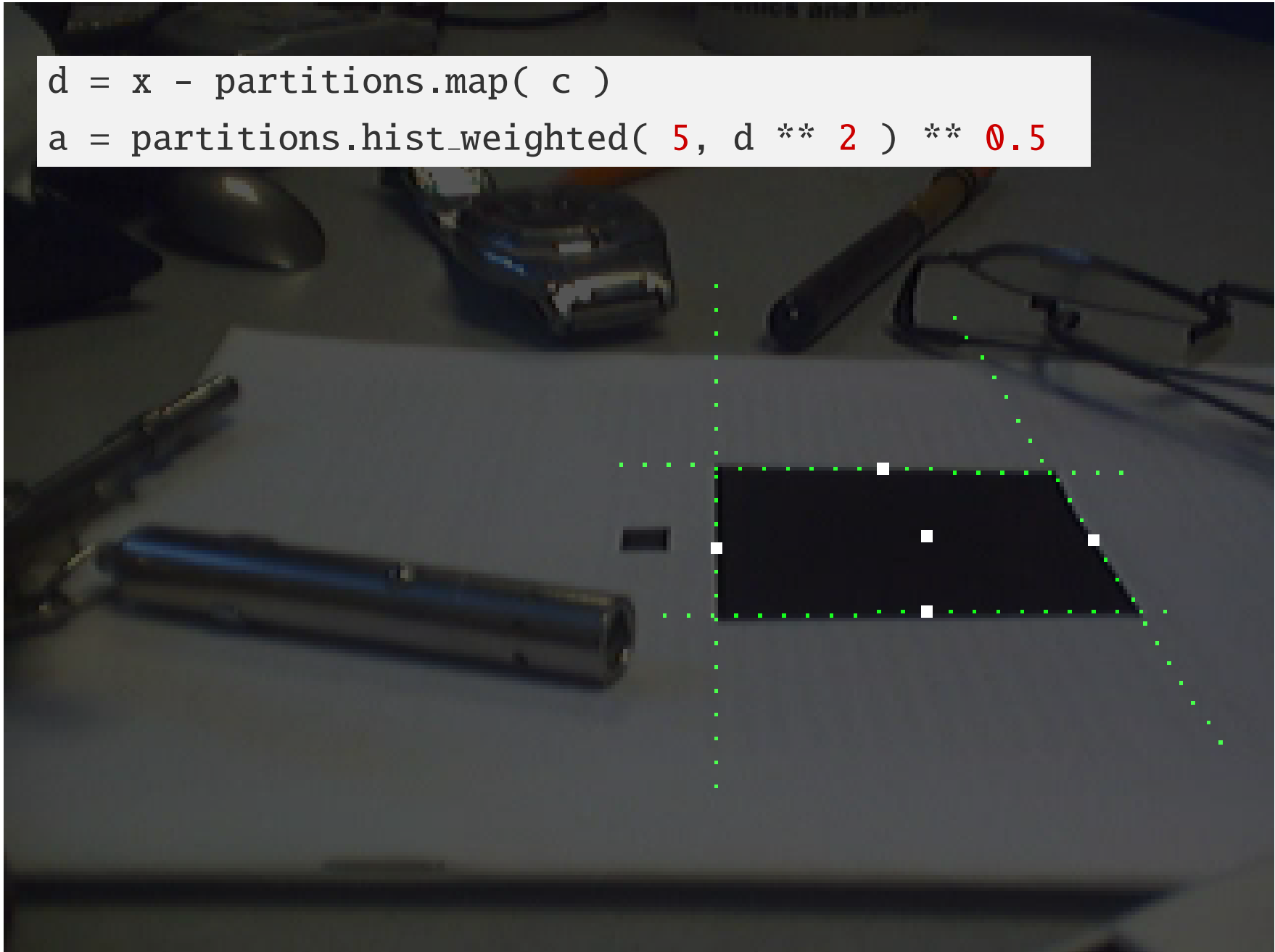




# Augmented Reality Example

## Angle of each Line

```
d = x - partitions.map( c )  
a = partitions.hist_weighted( 5, d ** 2 ) ** 0.5
```





# Augmented Reality Example

## Intersections

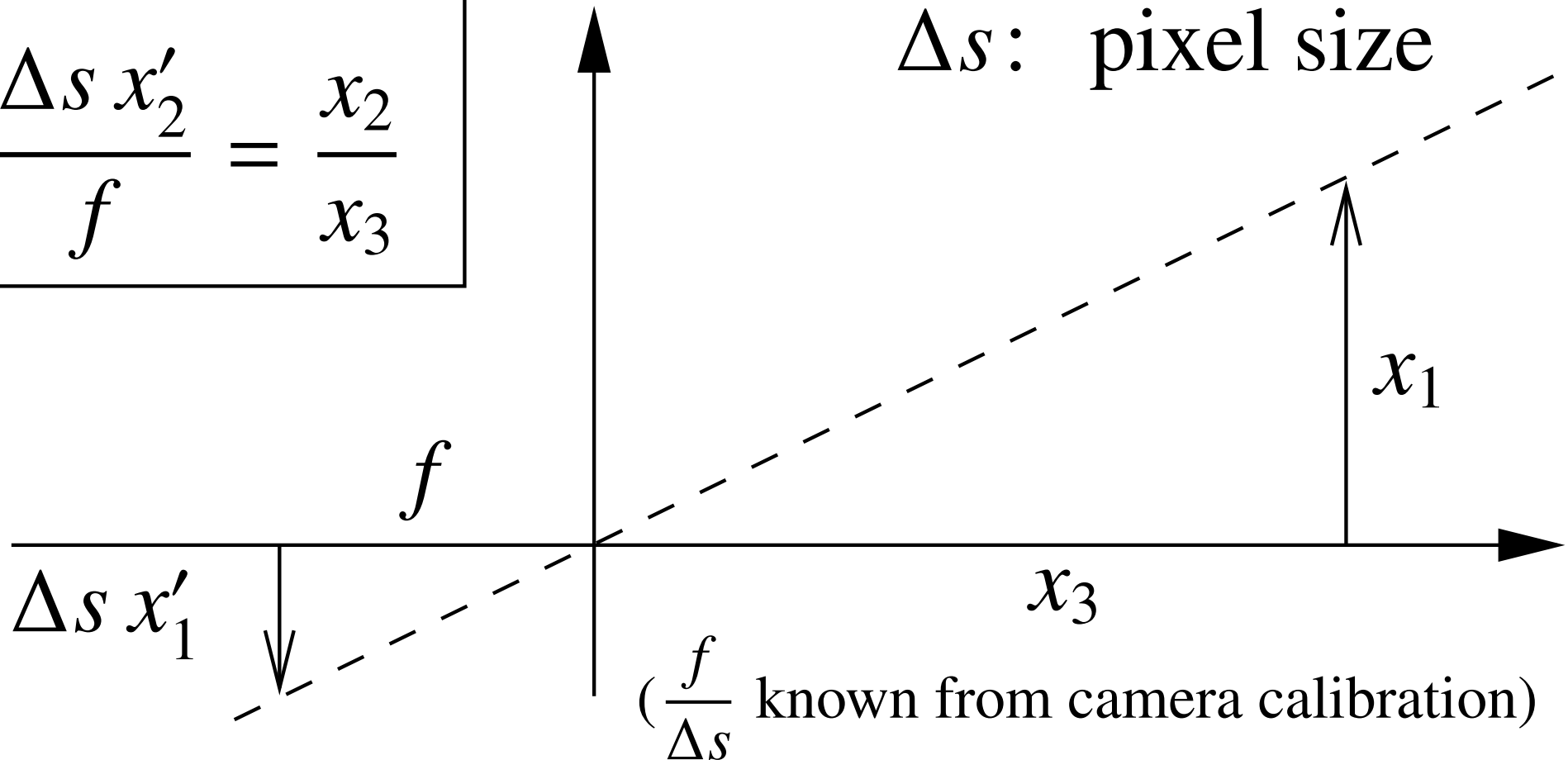
```
ms = Sequence[ *( 0 ... 4 ).collect do |i|  
  i1, i2 = i + 1, ( i + 1 ) % 4 + 1  
  l1, a1, l2, a2 = c[i1], a[i1], c[i2], a[i2]  
  ( l1 * a1.conj * a2 - l2 * a1 * a2.conj -  
    l1.conj * a1 * a2 + l2.conj * a1 * a2 ) /  
    ( a1.conj * a2 - a1 * a2.conj )  
end ] - 0.5 * Complex( *grey.shape )
```

```
s = 0.05 # meter  
m = Sequence[ Complex( -1, -1 ), Complex( 1, -1 ),  
  Complex( 1, 1 ), Complex( -1, 1 ) ] * s / 2
```



## 3D Pose: Pinhole Camera Model

$$\frac{\Delta s \, x_2'}{f} = \frac{x_2}{x_3}$$

 $\Delta s$ : pixel size



# Augmented Reality Example

## 3D Pose: Homogeneous Coordinates

$$x_3 x'_1 = \frac{f}{\Delta s} x_1$$
$$x_3 x'_2 = \frac{f}{\Delta s} x_2$$

$$\lambda x'_1 = \frac{f}{\Delta s} x_1$$
$$\Leftrightarrow \exists \lambda \in \mathbb{R}/\{0\} : \lambda x'_2 = \frac{f}{\Delta s} x_2$$
$$\lambda = x_3$$

$$\Leftrightarrow \exists \lambda \in \mathbb{R}/\{0\} : \lambda \begin{pmatrix} x'_1 \\ x'_2 \\ 1 \end{pmatrix} = \underbrace{\begin{pmatrix} f/\Delta s & 0 & 0 \\ 0 & f/\Delta s & 0 \\ 0 & 0 & 1 \end{pmatrix}}_{\text{intrinsic camera parameters}} \begin{pmatrix} x_1 \\ x_2 \\ x_3 \end{pmatrix}$$



# Augmented Reality Example

## 3D Pose: (Additional) Affine Transform

$$\exists \lambda \in \mathbb{R}/\{0\} : \lambda \begin{pmatrix} x'_1 \\ x'_2 \\ 1 \end{pmatrix} = \begin{pmatrix} f/\Delta s & 0 & 0 \\ 0 & f/\Delta s & 0 \\ 0 & 0 & 1 \end{pmatrix} \left( \begin{pmatrix} r_{11} & r_{12} & r_{13} \\ r_{21} & r_{22} & r_{23} \\ r_{31} & r_{32} & r_{33} \end{pmatrix} \begin{pmatrix} x_1 \\ x_2 \\ x_3 \end{pmatrix} + \begin{pmatrix} t_1 \\ t_2 \\ t_3 \end{pmatrix} \right)$$

$$\Leftrightarrow \exists \lambda \in \mathbb{R}/\{0\} : \lambda \begin{pmatrix} x'_1 \\ x'_2 \\ 1 \end{pmatrix} = \begin{pmatrix} f/\Delta s & 0 & 0 \\ 0 & f/\Delta s & 0 \\ 0 & 0 & 1 \end{pmatrix} \underbrace{\begin{pmatrix} r_{11} & r_{12} & r_{13} & t_1 \\ r_{21} & r_{22} & r_{23} & t_2 \\ r_{31} & r_{32} & r_{33} & t_3 \end{pmatrix}}_{\text{extrinsic camera parameters}} \begin{pmatrix} x_1 \\ x_2 \\ x_3 \\ 1 \end{pmatrix}$$

$$\begin{pmatrix} x'_1 \\ x'_2 \end{pmatrix} \text{ is } \begin{pmatrix} m'_{11} \\ m'_{12} \end{pmatrix}, \begin{pmatrix} m'_{21} \\ m'_{22} \end{pmatrix}, \dots, \begin{pmatrix} m'_{41} \\ m'_{42} \end{pmatrix} \text{ and } \begin{pmatrix} x_1 \\ x_2 \\ x_3 \end{pmatrix} \text{ is } \begin{pmatrix} m_{11} \\ m_{12} \\ 0 \end{pmatrix}, \begin{pmatrix} m_{21} \\ m_{22} \\ 0 \end{pmatrix}, \dots, \begin{pmatrix} m_{41} \\ m_{42} \\ 0 \end{pmatrix}$$



# Augmented Reality Example

## 3D Pose: Planar Homography I/II

Problem: Minimize  $\epsilon_{ij}$

$$\exists \lambda_i \in \mathbb{R}/\{0\} : \lambda_i \begin{pmatrix} m'_{i1} \\ m'_{i2} \\ 1 \end{pmatrix} + \begin{pmatrix} \epsilon_{i1} \\ \epsilon_{i2} \\ 0 \end{pmatrix} = \begin{pmatrix} f/\Delta s & 0 & 0 \\ 0 & f/\Delta s & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} r_{11} & r_{12} & r_{13} & t_1 \\ r_{21} & r_{22} & r_{23} & t_2 \\ r_{31} & r_{32} & r_{33} & t_3 \end{pmatrix} \begin{pmatrix} m_{i1} \\ m_{i2} \\ 0 \\ 1 \end{pmatrix}$$

$$\Leftrightarrow \exists \lambda_i \in \mathbb{R}/\{0\} : \lambda_i \begin{pmatrix} m'_{i1} \\ m'_{i2} \\ 1 \end{pmatrix} + \begin{pmatrix} \epsilon_{i1} \\ \epsilon_{i2} \\ 0 \end{pmatrix} = \underbrace{\begin{pmatrix} f/\Delta s & 0 & 0 \\ 0 & f/\Delta s & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} r_{11} & r_{12} & t_1 \\ r_{21} & r_{22} & t_2 \\ r_{31} & r_{32} & t_3 \end{pmatrix}}_{=:\mathcal{H}} \begin{pmatrix} m_{i1} \\ m_{i2} \\ 1 \end{pmatrix}$$

$$\Leftrightarrow \exists \lambda_i \in \mathbb{R}/\{0\} : \lambda_i \begin{pmatrix} m'_{i1} \\ m'_{i2} \\ 1 \end{pmatrix} + \begin{pmatrix} \epsilon_{i1} \\ \epsilon_{i2} \\ 0 \end{pmatrix} = \begin{pmatrix} h_{11} & h_{12} & h_{13} \\ h_{21} & h_{22} & h_{23} \\ h_{31} & h_{32} & h_{33} \end{pmatrix} \begin{pmatrix} m_{i1} \\ m_{i2} \\ 1 \end{pmatrix}, i \in \{1, 2, \dots, 4\}$$



# Augmented Reality Example

## 3D Pose: Planar Homography II/II

$$\Leftrightarrow \underbrace{(h_{31} m_{i1} + h_{32} m_{i2} + h_{33})}_{\lambda_i} \left( \begin{pmatrix} m'_{i1} \\ m'_{i2} \end{pmatrix} + \begin{pmatrix} \epsilon_{i1} \\ \epsilon_{i2} \end{pmatrix} \right) = \begin{pmatrix} h_{11} & h_{12} & h_{13} \\ h_{21} & h_{22} & h_{33} \end{pmatrix} \begin{pmatrix} m_{i1} \\ m_{i2} \\ 1 \end{pmatrix}$$

assuming  $\lambda_1 \approx \lambda_2 \approx \dots \approx \lambda_4$

this is approximately the same as

**Problem: Minimize  $\tilde{\epsilon}_{ij}$**

$$(h_{31} m_{i1} + h_{32} m_{i2} + h_{33}) \begin{pmatrix} m'_{i1} \\ m'_{i2} \end{pmatrix} + \begin{pmatrix} \tilde{\epsilon}_{i1} \\ \tilde{\epsilon}_{i2} \end{pmatrix} = \begin{pmatrix} h_{11} & h_{12} & h_{13} \\ h_{21} & h_{22} & h_{33} \end{pmatrix} \begin{pmatrix} m_{i1} \\ m_{i2} \\ 1 \end{pmatrix}$$

$$\Leftrightarrow \begin{pmatrix} \tilde{\epsilon}_{i1} \\ \tilde{\epsilon}_{i2} \end{pmatrix} = \begin{pmatrix} h_{11} & h_{12} & h_{13} \\ h_{21} & h_{22} & h_{33} \end{pmatrix} \begin{pmatrix} m_{i1} \\ m_{i2} \\ 1 \end{pmatrix} - (h_{31} m_{i1} + h_{32} m_{i2} + h_{33}) \begin{pmatrix} m'_{i1} \\ m'_{i2} \end{pmatrix}$$





# Augmented Reality Example

## 3D Pose: Singular Value Decomposition

$$\underbrace{\begin{pmatrix} m_{11} & m_{12} & 1 & 0 & 0 & 0 & -m'_{11}m_{11} & -m'_{11}m_{12} & -m'_{11} \\ 0 & 0 & 0 & m_{11} & m_{12} & 1 & -m'_{12}m_{11} & -m'_{12}m_{12} & -m'_{12} \\ m_{21} & m_{22} & 1 & 0 & 0 & 0 & -m'_{21}m_{21} & -m'_{21}m_{22} & -m'_{21} \\ 0 & 0 & 0 & m_{21} & m_{22} & 1 & -m'_{22}m_{21} & -m'_{22}m_{22} & -m'_{22} \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ m_{41} & m_{42} & 1 & 0 & 0 & 0 & -m'_{41}m_{41} & -m'_{41}m_{42} & -m'_{41} \\ 0 & 0 & 0 & m_{41} & m_{42} & 1 & -m'_{42}m_{41} & -m'_{42}m_{42} & -m'_{42} \end{pmatrix}}_{=:\mathcal{M}} \underbrace{\begin{pmatrix} h_{11} \\ h_{12} \\ \vdots \\ h_{33} \end{pmatrix}}_{=:\vec{h}} = \begin{pmatrix} \tilde{\epsilon}_{11} \\ \tilde{\epsilon}_{12} \\ \tilde{\epsilon}_{21} \\ \tilde{\epsilon}_{22} \\ \vdots \\ \tilde{\epsilon}_{41} \\ \tilde{\epsilon}_{42} \end{pmatrix}$$

$\|\vec{h}\| = \mu \neq 0$  to avoid trivial solution

I.e. find  $\vec{h} \in \mathbb{R}^9$  :  $\|\mathcal{M}\vec{h}\|$  minimal and  $\|\vec{h}\| = \mu$

**Solution:** Perform **SVD**  $\mathcal{M} = \mathcal{U}\Sigma\mathcal{V}^*$  and choose  $\vec{h} = \mu \vec{v}_9$  where  $\vec{v}_9$  is right-handed singular vector with the smallest singular value  $\sigma_9$



# Augmented Reality Example

## 3D Pose: 3D Homography

$$\mathcal{H} = \mu \begin{pmatrix} v_{91} & v_{92} & v_{93} \\ v_{94} & v_{95} & v_{96} \\ v_{97} & v_{98} & v_{99} \end{pmatrix} = \begin{pmatrix} f/\Delta s & 0 & 0 \\ 0 & f/\Delta s & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} r_{11} & r_{12} & t_1 \\ r_{21} & r_{22} & t_2 \\ r_{31} & r_{32} & t_3 \end{pmatrix}$$

$$\|\vec{r}_1\| = \|\vec{r}_2\| = 1$$

$$\vec{r}_3 = \vec{r}_1 \times \vec{r}_2$$

$$t_3 > 0$$

$$\vec{r}_3^\top \vec{t} \leq 0$$

$\Rightarrow$  Enough information to estimate 3D homography!



# Augmented Reality Example

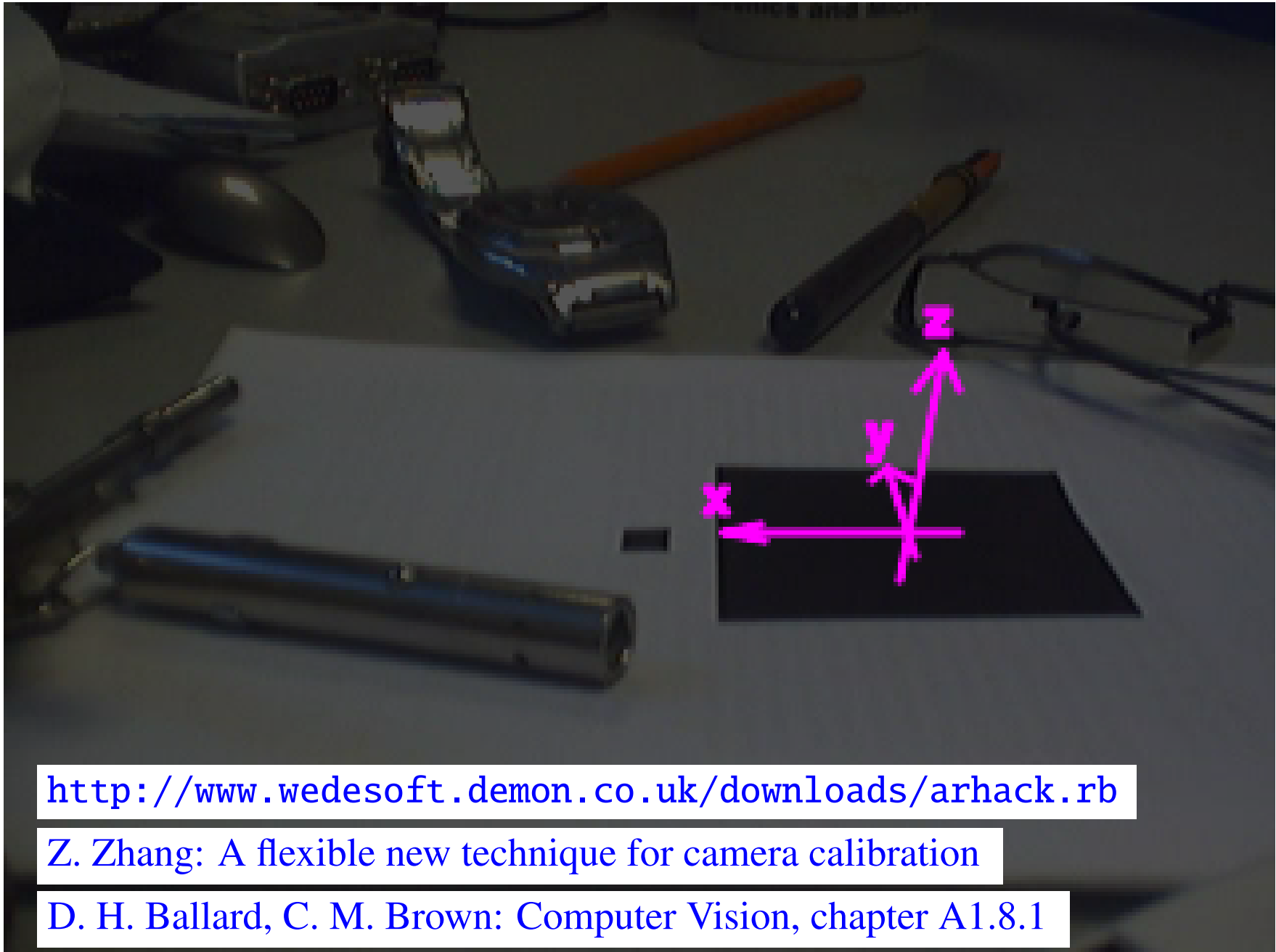
## Source Code

```
constraints = []
for i in 0 ... 4 do
  constraints.push [ m[i].real, m[i].imag, 1.0, 0.0, 0.0, 0.0,
    -ms[i].real * m[i].real, -ms[i].real * m[i].imag, -ms[i].real ]
  constraints.push [ 0.0, 0.0, 0.0, m[i].real, m[i].imag, 1.0,
    -ms[i].imag * m[i].real, -ms[i].imag * m[i].imag, -ms[i].imag ]
end
h = Matrix[ *constraints ].svd[ 2 ].row( 8 ).reshape 3, 3
fs = 1.2 * 320 # focal length divided by pixel size
intr = Matrix[ [ fs, 0.0, 0.0 ], [ 0.0, fs, 0.0 ], [ 0.0, 0.0, 1.0 ] ]
rt = intr.inv * h
scale = 0.5 * ( rt.column( 0 ).norm + rt.column( 1 ).norm )
t = rt.column( 2 ) / scale
e1, e2 = rt.column( 0 ).normalise, e2 = rt.column( 1 ).normalise
e3 = e1.x e2
e1, e2, e3 = -e2, e1, -e3 if e3.inner_product( t ) > 0
extr = Matrix[ [ e1[0], e2[0], e3[0], t[0] ], [ e1[1], e2[1], e3[1], t[1] ],
  [ e1[2], e2[2], e3[2], t[2] ], [ 0.0, 0.0, 0.0, 1.0 ] ]
```



# Augmented Reality Example

## Result



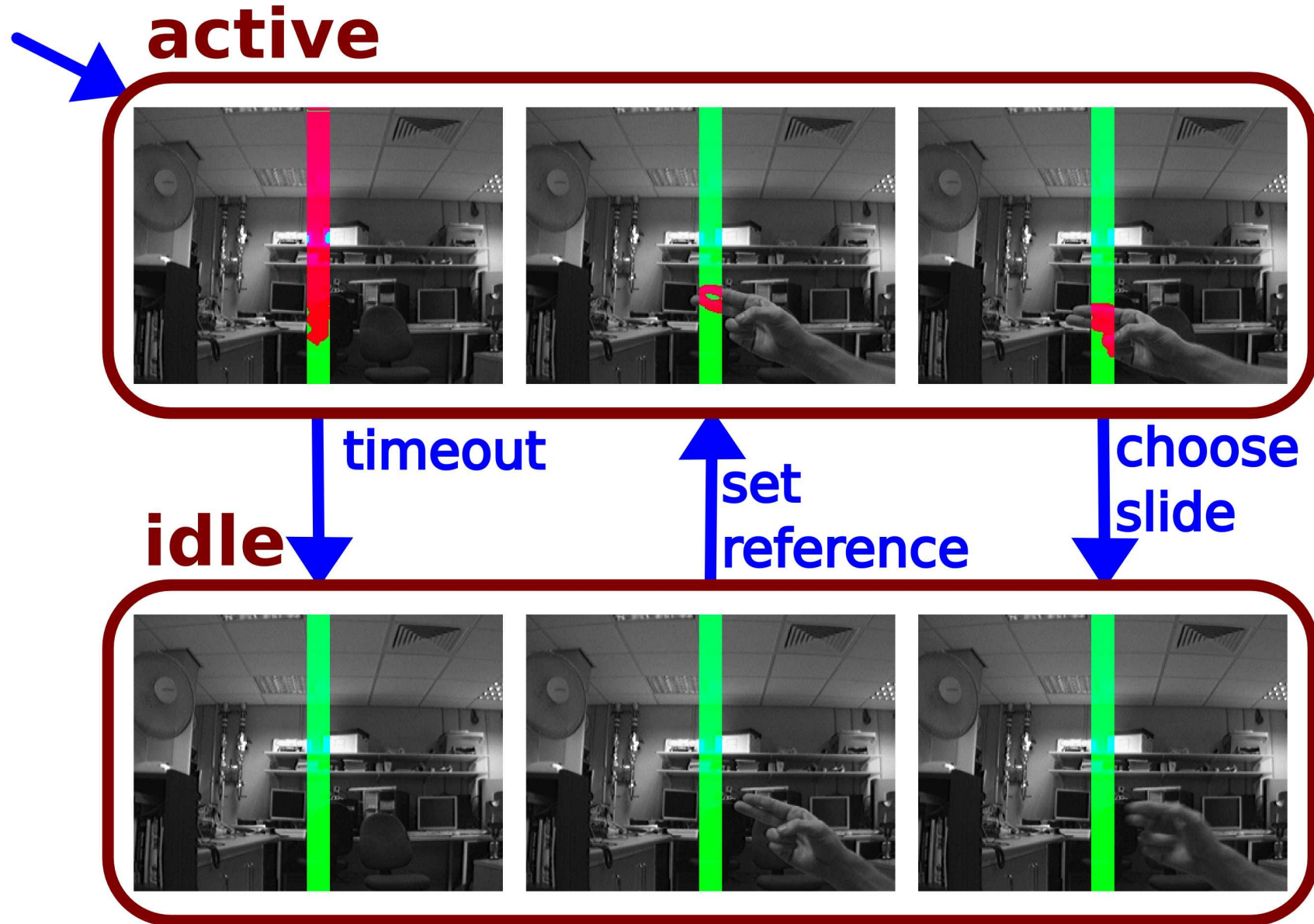
<http://www.wedesoft.demon.co.uk/downloads/arhack.rb>

Z. Zhang: A flexible new technique for camera calibration

D. H. Ballard, C. M. Brown: Computer Vision, chapter A1.8.1



# Presenter States



<http://www.wedesoft.demon.co.uk/downloads/sensor.rb>



# Presenter

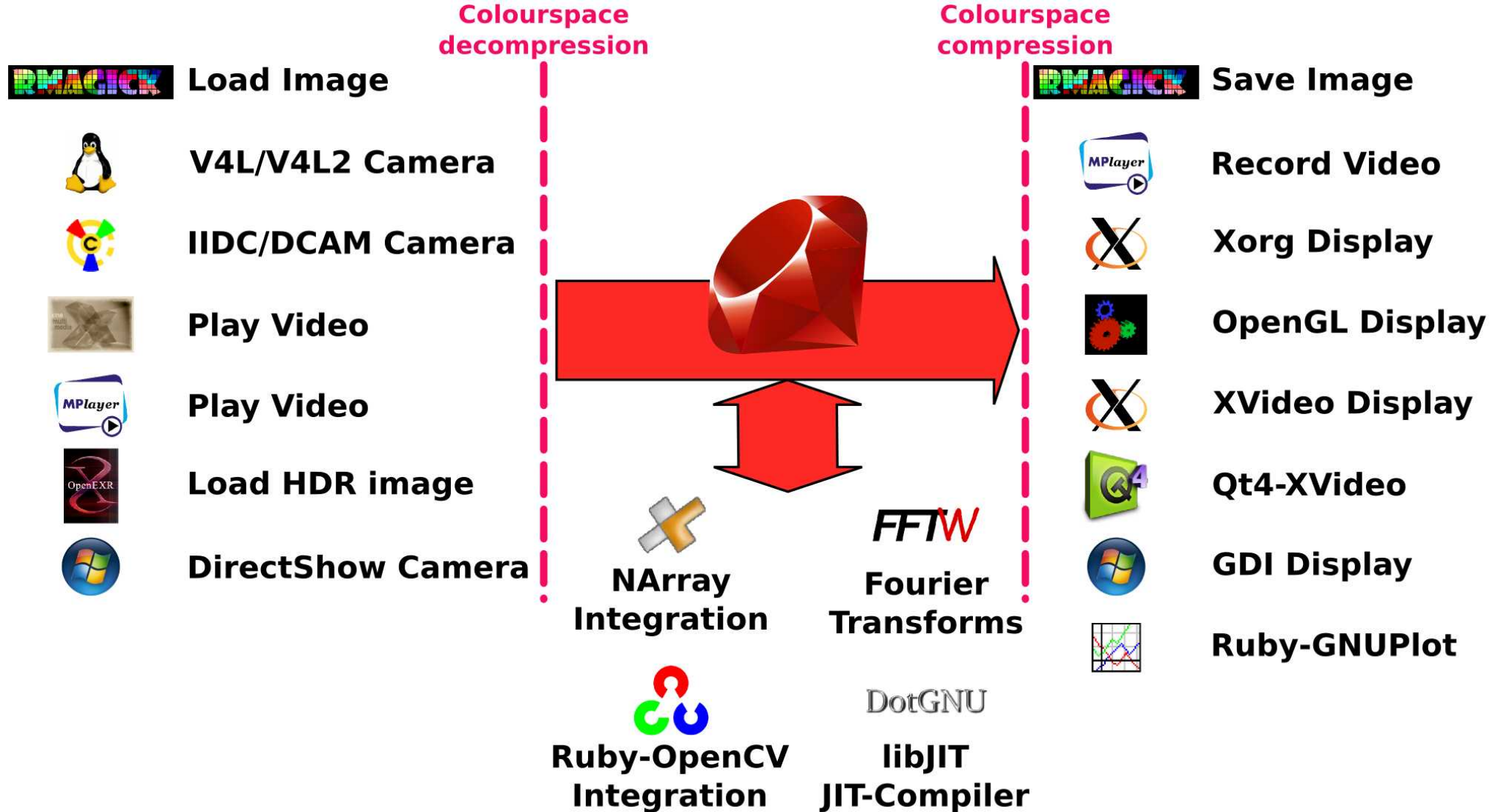
## Source Code (simplified)

```
input = DC1394Input.new
w, h, o = 20, input.height, input.width / 2 - 10
box = [ o ... o + w, 0 ... h ]
15.times { input.read }; bg = input.read_ubyte[ *box ]
ramp = Sequence.int( h ).indgen!.repmat( w ).roll
X11Display.show do
  img = input.read_ubytergb
  slice = ( img[ *box ].to_sint - bg ).gauss_blur( 2 ).abs >= 12
  n = slice.to_ubyte.sum
  if n > 20
    y = ramp.mask( slice ).sum / n
    print "#{ "%4d" % y }\r" ; STDOUT.flush
  end
  img[ *box ].r = slice.to_ubyte * 255
  img[ *box ].g = slice.not.to_ubyte * 255
  img
end
```





# Input/Output





# Closures

Python  
+  
OpenCV

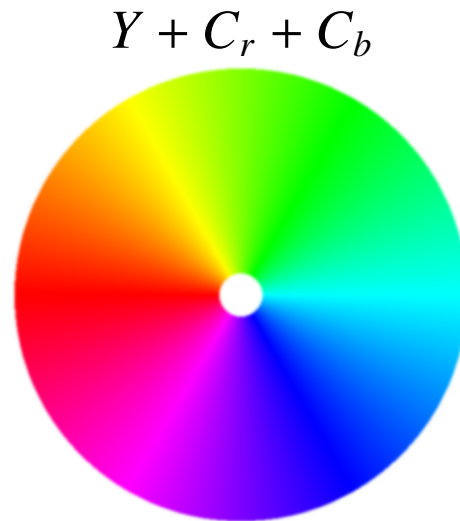
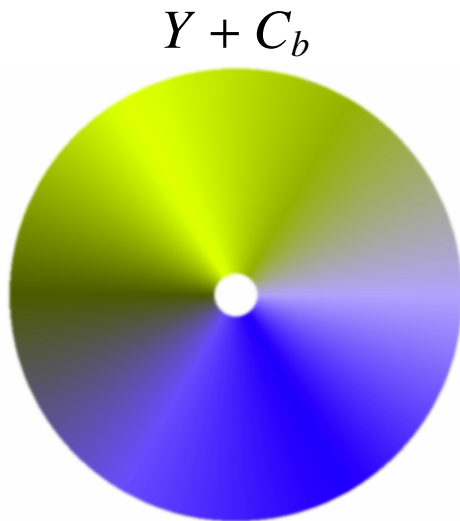
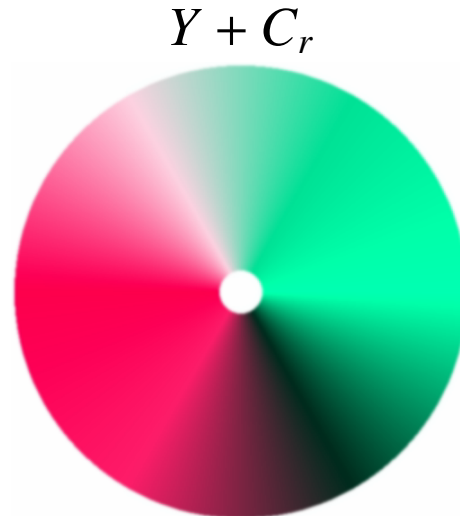
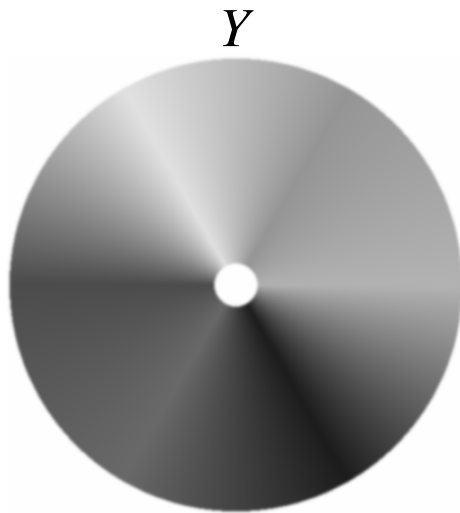
```
import sys
from opencv import cv
from opencv import highgui
highgui.cvNamedWindow( 'Camera' )
capture = highgui.cvCreateCameraCapture( -1 )
while 1:
    frame = highgui.cvQueryFrame( capture )
    gray = cv.cvCreateImage( cv.cvSize( frame.width, frame.height), 8, 1 )
    cv.cvCvtColor( frame, gray, cv.CV_BGR2GRAY )
    highgui.cvShowImage( 'Camera', gray )
    if highgui.cvWaitKey( 5 ) > 0:
        break
```

Ruby  
+  
HornetsEye

```
require 'hornetseye'
include Hornetseye
capture = V4L2Input.new
X11Display.show( :title => 'Camera' ) { capture.read.to_ubyte }
```



# Colourspace Conversions



	Channel	Resolution
$Y$	Luminance	high
$C_r$	Chroma red	low
$C_b$	Chroma blue	low

See also: <http://fourcc.org/>

$$\begin{pmatrix} Y \\ C_b \\ C_r \end{pmatrix} = \begin{pmatrix} 0.299 & 0.587 & 0.114 \\ -0.168736 & -0.331264 & 0.500 \\ 0.500 & -0.418688 & -0.081312 \end{pmatrix} \begin{pmatrix} R \\ G \\ B \end{pmatrix} + \begin{pmatrix} 0 \\ 128 \\ 128 \end{pmatrix}$$



# Lazy Computation

```
class Seq
  def Seq.new( *arr )
    unless Thread.current[ :lazy ]
      super *arr
    else
      Lazy.new( *arr ) { |x| x }
    end
  end
  def initialize( *arr )
    @arr = arr
  end
  def -@
    Seq.new *@arr.collect { |x| -x }
  end
end
```

```
class Lazy
  def initialize( *arr, &p )
    @arr, @p = arr, p
  end
  def demand
    Seq.new *@arr.collect { |i| @p.call i }
  end
  def -@
    Lazy.new( *@arr ) { |i| -@p.call( i ) }
  end
end
def lazy
  previous = Thread.current[ :lazy ]
  Thread.current[ :lazy ] = true
  retval = yield
  Thread.current[ :lazy ] = previous
  retval.demand
end
```



# Credits

## Credits

Aiden Lockwood, Aleksey Demakov, Annemie Wedekind, Balasundram Amavasai, Beverly Inkson, Chinwe Lucy Ozoegwu, Damien Douxchamps, Daniel Martín Marín, Géraud De La Mensbruge, Gerhard Wedekind, Hussein Abdul-Rahman, Jing Jing Wang, Jon Travis, Jong Peng, Juan Roldan, Julien Demarest, Julien Faucher, Julien Lacheray, Ken Dutton, Kim Chuan Lim, Kirill Kononenko, Klaus Treichel, Manuel Boissenin, Martin Howarth, Matthias Stumpf, Michael Doronin, Ralph Gay, Richard Dale, Sonia Fernández Rodríguez, Tan Kang Song, Ushakiran Soutapalli, Volkan Karaca, Warren Jasper, Zineb Saghi, ...

<http://www.wedesoft.demon.co.uk/hornetseye-api/>

<http://rubyforge.org/projects/hornetseye/>

<http://sourceforge.net/projects/hornetseye/>

<http://launchpad.net/hornetseye/>

<http://raa.ruby-lang.org/project/hornetseye/>

<http://www.ohloh.net/p/hornetseye/>